

Rie-nam(e): Key

AP Calculus AB: 7.5 Riemann Practice

1. Write out the formulas for the Riemann Sums of the function  $h(x)$  for the interval  $[2,4]$  with 4 rectangles for each of the methods below.

$B = \frac{4-2}{4} = .5$

a) Left-hand Rule

$.5[h(2) + h(2.5) + h(3) + h(3.5)]$

b) Right-hand Rule

$.5[h(4) + h(3.5) + h(3) + h(2.5)]$

c) Midpoint Rule

$.5[h(2.25) + h(2.75) + h(3.25) + h(3.75)]$

d) Trapezoid Rule

$\frac{.5}{2}[h(2) + 2h(2.5) + 2h(3) + 2h(3.5) + h(4)]$

2. The function  $f(x) = x^2$  is increasing whenever  $x > 0$ . If you use right-hand rule to estimate the integral of  $f(x)$  for the interval  $[3,15]$ , would that be an over or under-estimate? Why?

*over estimation*

3. If you use left-hand rule to approximate the area under the curve of the function  $g(x) = \ln(x) + 1$  for the interval  $[1,5]$  would you be over or under-estimating the integral? Why?

*under estimation*

4. Write out the formulas for the Riemann Sums of the function  $y(x)$  for the interval  $[0.5,1.7]$  with 6 rectangles for each of the methods below.

a) Left-hand Rule

$.2[f(.5) + f(.7) + f(.9) + f(1.1) + f(1.3) + f(1.5)]$

b) Right-hand Rule

$.2[f(1.7) + f(1.5) + f(1.3) + f(1.1) + f(.9) + f(.7)]$

c) Midpoint Rule

$.2[f(.6) + f(.8) + f(1) + f(1.2) + f(1.4) + f(1.6)]$

d) Trapezoid Rule

$\frac{.2}{2}[f(.5) + 2f(.7) + 2f(.9) + 2f(1.1) + 2f(1.3) + 2f(1.5) + f(1.7)]$

5. Estimate the area under the curve of the function in the table below using right-hand rule for the interval  $[0,4]$  using 3 rectangles.

x	0	1	3	4
f(x)	5	7	9	12

*unequal bases*

$(1)(7) + (2)(9) + (1)(12) = 7 + 18 + 12 = 37$

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6. Using the table below answer the questions underneath.

x	0	0.5	1	1.5	2	2.5	3
f(x)	2	3.125	4.5	6.125	8	10.125	12.5

a) Estimate the area under the curve of the function represented in the table for the interval  $[0,2]$  using the trapezoidal method of estimation with 4 trapezoids.

$$B = \frac{2-0}{4} = .5$$

$$A = \frac{.5}{2} [f(0) + 2f(.5) + 2f(1) + 2f(1.5) + f(2)] \\ = .25 [2 + 2(3.125) + 2(4.5) + 2(6.125) + 8] = \boxed{9.375}$$

b) Estimate the integral of the function shown in the table using the midpoint method of approximation for the interval  $[0,3]$  using 3 rectangles.

$$B = \frac{3-0}{3} = 1$$

$$A = 1 [f(.5) + f(1.5) + f(2.5)] = 1 [3.125 + 6.125 + 10.125] = \boxed{19.375}$$

c) Approximate the area under the curve of the function  $f(x)$  using the left-hand method of estimation for the interval  $[0,3]$  using 6 rectangles.

$$B = \frac{3-0}{6} = .5$$

$$A = .5 [f(0) + f(.5) + f(1) + f(1.5) + f(2) + f(2.5)] \\ = .5 [2 + 3.125 + 4.5 + 6.125 + 8 + 10.125] = \boxed{16.938}$$

d) Find the area under the curve of the function using the left-hand approximation for the interval  $[0,3]$  using 2 rectangles.

$$B = \frac{3-0}{2} = 1.5$$

$$1.5 [f(0) + f(1.5)] = 1.5 [2 + 6.125] = \boxed{12.188}$$

e) The derivative of the function shown in the table is  $f'(x) = x + 2$  find the particular solution of the function  $f(x)$ .

$$\int x+2 dx$$

$$f(x) = \frac{x^2}{2} + 2x + C$$

$$2 = \frac{0^2}{2} + 2(0) + C$$

$$2 = C$$

f) Find  $f(3)$ .

$$f(3) = \frac{(3)^2}{2} + 2(3) + 2 = \frac{9}{2} + 6 + 2 = \frac{9}{2} + \frac{12}{2} + \frac{4}{2} = \boxed{\frac{25}{2}}$$

$$f(x) = \frac{x^2}{2} + 2x + 2$$