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AP Calculus AB: 1.1 Algebra 1 Review

Find the equation, in slope-intercept form, of the line formed by two points.

$$1) \begin{matrix} x_1 & y_1 & x_2 & y_2 \\ (-4, -8), & (2, 7) \end{matrix}$$
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - (-8)}{2 - (-4)} = \frac{15}{6} = \frac{5}{2}$$

$$(y - y_1) = m(x - x_1)$$
$$y - (-8) = \frac{5}{2}(x - (-4))$$
$$y + 8 = \frac{5}{2}x + 10 \Rightarrow \boxed{y = \frac{5}{2}x + 2}$$

$$2) (-3, -\frac{3}{2}), (4, -5)$$
$$m = \frac{-5 - (-\frac{3}{2})}{4 - (-3)} = \frac{-\frac{7}{2}}{7} = -\frac{1}{2}$$

$$y - (-5) = -\frac{1}{2}(x - 4)$$
$$y + 5 = -\frac{1}{2}x + 2$$
$$\boxed{y = -\frac{1}{2}x - 3}$$

$$3) (5, \frac{8}{3}), (0, 6)$$
$$m = \frac{\frac{8}{3} - 6}{5 - 0} = \frac{-\frac{10}{3}}{5} = -\frac{2}{3}$$

$$y - 6 = -\frac{2}{3}(x - 0)$$
$$y - 6 = -\frac{2}{3}x$$
$$\boxed{y = -\frac{2}{3}x + 6}$$

Solve for the missing variables.

$$4) 10(x + 5) - 20x = 5x - (2x + 28)$$
$$10x + 50 - 20x = 5x - 2x - 28$$
$$-10x + 50 = 3x - 28$$
$$78 = 13x$$
$$\boxed{x = 6}$$

$$5) x^2 + 4x - 10 = 2x + 5$$
$$x^2 + 2x - 15 = 0$$
$$(x - 3)(x + 5) = 0$$
$$\boxed{x = 3} \quad \boxed{x = -5}$$

$$6) 2(x^2 + 3x) = -x + 15$$
$$2x^2 + 6x = -x + 15$$
$$2x^2 + 7x - 15 = 0$$
$$(x + 5)(2x - 3) = 0$$
$$\boxed{x = -5} \quad \boxed{x = \frac{3}{2}}$$

$$7) \frac{\ln(x) + 6}{2} = 3$$
$$\ln(x) + 6 = 6$$
$$e^{\ln(x)} = e^0$$
$$\boxed{x = e^0 = 1}$$

$$8) \frac{e^{x+5}}{2} = 3$$
$$e^{x+5} = 6$$
$$\ln(e)^x = \ln(1)$$
$$\boxed{x = \ln(1) = 0}$$

$$9) \ln(5x) = 0$$
$$5x = e^0 = 1$$
$$5x = 1$$
$$\boxed{x = \frac{1}{5}}$$

$$10) e^{2x+4} = 1$$
$$\ln(e^{2x+4}) = \ln(1)$$
$$2x + 4 = 0$$
$$2x = -4$$
$$\boxed{x = -2}$$

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Simplify each of the following equations

$$11) \frac{x^2-4x-12}{x^2+7x+10} = \frac{(x-6)\cancel{(x+2)}}{\cancel{(x+5)}(x+5)}$$

$$\boxed{\frac{x-6}{x+5}}$$

$$12) \frac{3x^2+2x-21}{2x^2+11x+15} = \frac{(3x-7)\cancel{(x+3)}}{(2x+5)\cancel{(x+3)}} =$$

$$\boxed{\frac{3x-7}{2x+5}}$$

$$13) \frac{x^2-4}{2x^2+8x+8} = \frac{(x+2)\cancel{(x-2)}}{2(x^2+4x+4)}$$

$$= \frac{(x+2)\cancel{(x-2)}}{2\cancel{(x+2)}(x+2)} = \boxed{\frac{x-2}{2(x+2)}}$$

$$14) \frac{x^4-16}{(x^2+4)(2x^2-x-10)} = \frac{(x^2-4)\cancel{(x^2+4)}}{\cancel{(x^2+4)}(x+2)(2x-5)}$$

$$\frac{x^2-4}{(x+2)(2x-5)} = \frac{\cancel{(x+2)}(x-2)}{\cancel{(x+2)}(2x-5)} = \boxed{\frac{x-2}{2x-5}}$$

Simplify each of the following polynomial equations

$$15) \frac{21k^3k^4}{1k^2} = \frac{3k^7}{k^2} = \boxed{3k^5}$$

$$16) \frac{(p^3)^{-2}k^2}{3p^{-2}} = \frac{p^{-6}k^2}{3p^{-2}} = \frac{p^2k^2}{3p^4} = \boxed{\frac{k^2}{3p^4}}$$

$$17) \frac{3(2xy^3)^3}{4x^{-2}y^6} = \frac{3(8x^3y^9)}{4x^{-2}y^6}$$

$$\frac{6x^3y^9x^2}{y^6} = \boxed{6x^5y^3}$$

$$18) \frac{2^2xyz}{zx^{-1}} = \frac{2xyz}{x^{-1}} = \boxed{2x^2yz}$$